

29.10 1)

$$5^{2x} = 2^{1-x} \Leftrightarrow \log 5^{2x} = \log 2^{1-x} \Leftrightarrow 2x \log 5 = (1-x) \log 2 \Leftrightarrow 2x \log 5 = \log 2 - x \log 2 \Leftrightarrow$$

$$\Leftrightarrow 2x \log 5 + x \log 2 = \log 2 \Leftrightarrow x(2 \log 5 + \log 2) = \log 2 \Leftrightarrow x = \frac{\log 2}{2 \log 5 + \log 2}$$

29.10 2)

$$7^{2x-1} = 2 \xRightarrow[2>0]{7^{2x-1}>0} \log 7^{2x-1} = \log 2 \Rightarrow (2x-1) \log 7 = \log 2 \Rightarrow$$

$$\Rightarrow 2x-1 = \frac{\log 2}{\log 7} \Rightarrow 2x = \frac{\log 2}{\log 7} + 1 \Rightarrow 2x = \frac{\log 2 + \log 7}{\log 7} \Rightarrow$$

$$\Rightarrow 2x = \frac{\log 14}{\log 7} \Rightarrow x = \frac{\log 14}{2 \log 7}$$

29.10 3)

$$3^{x+1} = 5 \xRightarrow[5>0]{3^{x+1}>0} \log 3^{x+1} = \log 5 \Rightarrow (x+1) \log 3 = \log 5 \Rightarrow$$

$$\Rightarrow x \log 3 = \log 5 - \log 3 \Rightarrow x = \frac{\log 5 - \log 3}{\log 3}$$

29.10 4)

$$2^x = 3^x \xRightarrow[3^x>0]{2^x>0} \log 2^x = \log 3^x \Rightarrow x \log 2 = x \log 3 \Rightarrow$$

$$\Rightarrow x(\log 2 - \log 3) = 0 \Rightarrow x = 0$$

29.10 5)

$$5^x = 3^{x-1} \xRightarrow[3^{x-1}>0]{5^x>0} \log 5^x = \log 3^{x-1} \Rightarrow x \log 5 = (x-1) \log 3 \Rightarrow$$

$$\Rightarrow x \log 5 = x \log 3 - \log 3 \Rightarrow x(\log 5 - \log 3) = -\log 3 \Rightarrow$$

$$\Rightarrow x = \frac{\log 3}{\log 3 - \log 5}$$

29.10 6)

$$4^{x-3} = 3^{x+2} \xRightarrow[3^{x+2}>0]{4^{x-3}>0} \log 4^{x-3} = \log 3^{x+2} \Rightarrow (x-3) \log 4 = (x+2) \log 3 \Rightarrow$$

$$\Rightarrow x \log 4 - 3 \log 4 = x \log 3 + 2 \log 3 \Rightarrow x(\log 4 - \log 3) = 2 \log 3 + 3 \log 4 \Rightarrow$$

$$x = \frac{2 \log 3 + 3 \log 4}{\log 4 - \log 3}$$

29.10 7)

$$2^{2x+1} = 5^{x-2} \xRightarrow[5^{x-2}>0]{2^{2x+1}>0} \log 2^{2x+1} = \log 5^{x-2} \Rightarrow (2x-1) \log 2 = (x-2) \log 5 \Rightarrow$$

$$\Rightarrow 2x \log 2 - \log 2 = x \log 5 - 2 \log 5 \Rightarrow x(2 \log 2 - \log 5) = \log 2 - 2 \log 5 \Rightarrow$$

$$x = \frac{2 \log 5 - \log 2}{\log 5 - 2 \log 2}$$