

21.3 1)

$$x^3 - 3x^2 - 4x + 12 = 0 \Rightarrow x^2(x-3) - 4(x-3) = 0 \Rightarrow (x-3)(x^2-4) = 0 \Rightarrow$$

$$\Rightarrow (x-3)(x-2)(x+2) = 0 \Rightarrow$$

$$\Rightarrow x-3=0$$

$$\Rightarrow x=3$$

$$\begin{array}{l} \text{ή} \quad x-2=0 \Rightarrow \\ \parallel \quad \Rightarrow x=2 \end{array}$$

$$\begin{array}{l} \text{ή} \quad x+2=0 \Rightarrow \\ \parallel \quad \Rightarrow x=-2 \end{array}$$

21.3 2)

$$x^3 + 2x^2 + 3x + 6 = 0 \Rightarrow x(x^2 + 3) + 2(x^2 + 3) = 0 \Rightarrow$$

$$\Rightarrow (x^2 + 3)(x+2) = 0 \Rightarrow x^2 + 3 = 0 \dots\dots \text{αδύνατη}$$

$$\text{ή} \quad x+2=0 \Rightarrow x=-2$$

21.3 3)

$$2x^3 + 8x^2 - 6x - 24 = 0 \Rightarrow 2x(x^2 - 3) + 8(x^2 - 3) = 0 \Rightarrow (x^2 - 3)(2x+8) = 0 \Rightarrow$$

$$\Rightarrow x^2 - 3 = 0$$

$$\Rightarrow 2x+8=0$$

$$\Rightarrow x^2 = 3$$

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$$\Rightarrow 2x = -8$$

$$\Rightarrow x = \pm\sqrt{3}$$

$$\Rightarrow x = -4$$

21.3 4)

$$x^5 + 4x^2 = 4x^3 + x^4 \Rightarrow x^5 + 4x^2 - 4x^3 - x^4 = 0 \Rightarrow$$

$$\Rightarrow x^4(x-1) - 4x^2(x-1) = 0 \Rightarrow (x-1)(x^4 - 4x^2) = 0 \Rightarrow$$

$$\Rightarrow (x-1) \cdot x^2 \cdot (x^2 - 4) = 0 \Rightarrow$$

$$\Rightarrow x-1=0$$

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$$\Rightarrow x^2 = 0$$

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$$\Rightarrow x^2 - 4 = 0$$

$$\Rightarrow x=1$$

$$\Rightarrow x=0$$

$$\Rightarrow x = \pm 2$$

21.3 5)

$$2x^5 + 9x^2 = x^4 + 18x^3 \Rightarrow 2x^5 - x^4 - 18x^3 + 9x^2 = 0 \Rightarrow$$

$$\Rightarrow x^4(2x-1) - 9x^2(2x-1) = 0 \Rightarrow (2x-1)(x^4 - 9x^2) = 0 \Rightarrow$$

$$\Rightarrow (2x-1) \cdot x^2 \cdot (x^2 - 9) = 0 \Rightarrow$$

$$\Rightarrow 2x-1=0$$

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$$\Rightarrow x^2 = 0$$

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$$\Rightarrow x^2 - 9 = 0$$

$$\Rightarrow x = \frac{1}{2}$$

$$\Rightarrow x=0$$

$$\Rightarrow x = \pm 3$$