

20.4 1)

$$\begin{array}{r|l}
 \cancel{x^3} + \alpha x^2 & + x & -3 \\
 \hline
 \cancel{-x^3} + x^2 & -2x & \\
 \hline
 (\alpha+1)\cancel{x^2} & -x & -3 \\
 \hline
 -(\alpha+1)\cancel{x^2} + (\alpha+1)x - 2\alpha - 2 & & \\
 \hline
 & \alpha x & -2\alpha - 5
 \end{array}$$

Επομένως $x^3 + \alpha x^2 + x - 3 = (x^2 - x + 2)(x + \alpha + 1) + \alpha x + 2\alpha - 1$

20.4 2)

$$\begin{array}{r|l}
 x^3 + 2x^2 + \alpha x - 2 & x^2 + x + 1 \\
 \hline
 -x^3 - x^2 - x & x + 1 \\
 \hline
 x^2 + (\alpha - 1)x - 2 & \\
 \hline
 -x^2 - x - 1 & \\
 \hline
 (\alpha - 2)x - 3 &
 \end{array}$$

Επομένως $x^3 + 2x^2 + \alpha x - 2 = (x^2 + x + 1)(x + 1) + (\alpha - 2)x - 3$

20.4 3)

$$\begin{array}{r|l}
 x^3 + \alpha x^2 - x + 5 & x^2 + x + 2 \\
 \hline
 -x^3 - x^2 - 2x & x + (\alpha - 1) \\
 \hline
 (\alpha - 1)x^2 - 3x + 5 & \\
 \hline
 -(\alpha - 1)x^2 - (\alpha - 1)x - 2\alpha + 2 & \\
 \hline
 (-\alpha - 2)x - 2\alpha + 7 &
 \end{array}$$

Επομένως $x^3 + \alpha x^2 - x + 5 = (x^2 + x + 2)(x + \alpha - 1) + (-\alpha - 2)x - 2\alpha + 7$

20.4 4)

$$\begin{array}{r|l}
 x^3 + \alpha x^2 - 2\alpha x + 4 & x^2 - x + 1 \\
 \hline
 -x^3 + x^2 - x & x + \alpha + 1 \\
 \hline
 (\alpha + 1)x^2 - (2\alpha + 1)x + 4 & \\
 \hline
 -(\alpha + 1)x^2 + (\alpha + 1)x - \alpha - 1 & \\
 \hline
 -\alpha x - \alpha + 3 &
 \end{array}$$

Επομένως $x^3 + \alpha x^2 - 2\alpha x + 4 = (x^2 - x + 1)(x + \alpha + 1) - \alpha x - \alpha + 3$

20.4 5)

$x^3 + (\alpha + 2)x^2 - \alpha x - 3$	$\frac{x^2 - x - 2}{x + \alpha + 3}$
$-x^3 + x^2 + 2x$	
$(\alpha + 3)x^2 + (2 - \alpha)x - 3$	
$-(\alpha + 3)x^2 + (3 + \alpha)x + 2\alpha + 6$	
$5x + 2\alpha + 3$	

Επομένως $x^3 + (\alpha + 2)x^2 - \alpha x - 3 = (x^2 - x - 2)(x + \alpha + 3) + 5x + 2\alpha + 3$

20.4 6)

$2x^3 - (\alpha + 1)x^2 + \alpha x + 1$	$\frac{x^2 - x + 3}{2x - \alpha + 1}$
$-2x^3 + 2x^2 - 6x$	
$(-\alpha + 1)x^2 + (\alpha - 6)x + 1$	
$-(-\alpha + 1)x^2 + (-\alpha + 1)x + 3\alpha - 3$	
$-5x + 3\alpha - 2$	

Επομένως $2x^3 - (\alpha + 1)x^2 + \alpha x + 1 = (x^2 - x + 3)(2x - \alpha + 1) - 5x + 3\alpha - 2$