

$$\begin{aligned}
 \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \frac{x}{\eta\mu^2 x} dx &= \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} x (-\sigma\varphi x)' dx = \left[-x\sigma\varphi x \right]_{\frac{\pi}{6}}^{\frac{\pi}{2}} - \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} (x)' (-\sigma\varphi x) dx = \\
 &= -\cancel{\frac{\pi}{2}\sigma\varphi\frac{\pi}{2}} + \frac{\pi}{6}\sigma\varphi\frac{\pi}{6} + \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \sigma\varphi x dx = \frac{\pi\sqrt{3}}{6} + \int_{\frac{\pi}{6}}^{\frac{\pi}{2}} \frac{\sigma\upsilon\nu x}{\eta\mu x} dx = \frac{\pi\sqrt{3}}{6} + \left[\ln|\eta\mu x| \right]_{\frac{\pi}{6}}^{\frac{\pi}{2}} = \\
 &= \frac{\pi\sqrt{3}}{6} + \ln\left|\eta\mu\frac{\pi}{2}\right| - \ln\left|\eta\mu\frac{\pi}{6}\right| = \frac{\pi\sqrt{3}}{6} + \ln\cancel{\left|\eta\mu\frac{\pi}{2}\right|} - \ln\frac{1}{2} = \frac{\pi\sqrt{3}}{6} + \ln 2
 \end{aligned}$$