

7.4 1)

$$\alpha) \lim_{x \rightarrow -\infty} \frac{2x^2 + 7x - 2}{6x^3 - 4x + 3} = \lim_{x \rightarrow -\infty} \frac{x^2 \left(2 + \frac{7}{x} - \frac{2}{x^2} \right)}{x^3 \left(6 - \frac{4}{x^2} + \frac{3}{x^3} \right)} = \frac{2 + 0 - 0}{(-\infty)(6 - 0 + 0)} = \frac{2}{-\infty} = \boxed{0}$$

$$\beta) \lim_{x \rightarrow +\infty} \frac{-3x^2 - 8x + 4}{5x^4 - 2x^3 + x - 1} = \lim_{x \rightarrow +\infty} \frac{x^2 \left(-3 - \frac{8}{x} + \frac{4}{x^2} \right)}{x^4 \left(5 - \frac{2}{x} + \frac{1}{x^3} - \frac{1}{x^4} \right)} = \frac{-3 - 0 + 0}{(+\infty)(5 - 0 + 0 - 0)} = \frac{-3}{+\infty} = \boxed{0}$$

7.4 2)

$$\lim_{x \rightarrow -\infty} \frac{-5x^3 + 3x^2}{x^5 + 1} = \lim_{x \rightarrow -\infty} \frac{x^3 \left(-5 + \frac{3}{x} \right)}{x^5 \left(1 + \frac{1}{x^5} \right)} = \frac{-5 + 0}{(-\infty)(1 + 0)} = \frac{-5}{-\infty} = \boxed{0}$$

7.4 3)

$$\lim_{x \rightarrow +\infty} \frac{-5x + 1}{x^4 + 8x - 1} = \lim_{x \rightarrow +\infty} \frac{x \left(-5 + \frac{1}{x} \right)}{x^4 \left(1 + \frac{8}{x} - \frac{1}{x^4} \right)} = \frac{-5 + 0}{(+\infty)(1 + 0 - 0)} = \frac{-5}{+\infty} = \boxed{0}$$

7.4 4)

$$\lim_{x \rightarrow -\infty} \frac{3x^3 + x^2 - 2x + 5}{x^4 - x^2 - x + 1} = \lim_{x \rightarrow -\infty} \frac{x^3 \left(3 + \frac{1}{x} - \frac{2}{x^2} + \frac{5}{x^3} \right)}{x^4 \left(1 - \frac{1}{x^2} - \frac{1}{x^3} + \frac{1}{x^4} \right)} = \frac{3 + 0 - 0 + 0}{(-\infty)(1 - 0 - 0 + 0)} = \frac{3}{-\infty} = 0$$

7.4 5)

$$\lim_{x \rightarrow +\infty} \frac{x^2 - 4x + 5}{x^3 + 7x^2 - 5x + 2} = \lim_{x \rightarrow +\infty} \frac{x^2 \left(1 - \frac{4}{x} + \frac{5}{x^2} \right)}{x^3 \left(1 + \frac{7}{x} - \frac{5}{x^2} + \frac{2}{x^3} \right)} = \frac{1 - 0 + 0}{(+\infty)(1 + 0 - 0 + 0)} = \frac{1}{+\infty} = 0$$