

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

7.10 1)

$$\alpha) \lim_{x \rightarrow +\infty} (7\sqrt{x} - 3) = \lim_{x \rightarrow +\infty} \sqrt{x} \left(7 - \frac{3}{\sqrt{x}} \right) = +\infty(7 - 0) = \boxed{+\infty}$$

$$\beta) \lim_{x \rightarrow +\infty} (2x - 3\sqrt{x} + 9) = \lim_{x \rightarrow +\infty} x \left(2 - \frac{3}{\sqrt{x}} + \frac{9}{x} \right) = +\infty(2 - 0 + 0) = \boxed{+\infty}$$

7.10 2)

$$\lim_{x \rightarrow +\infty} (4\sqrt{x} + 3) = \lim_{x \rightarrow +\infty} \sqrt{x} \left(4 + \frac{3}{\sqrt{x}} \right) = (+\infty)(4 + 0) = \boxed{+\infty}$$

7.10 3)

$$\lim_{x \rightarrow +\infty} (-2\sqrt{x} + 5) = \lim_{x \rightarrow +\infty} \sqrt{x} \left(-2 + \frac{5}{\sqrt{x}} \right) = (+\infty)(-2 + 0) = \boxed{-\infty}$$

7.10 4)

$$\boxed{\lim_{x \rightarrow +\infty} (7x - 4\sqrt{x})} = \lim_{x \rightarrow +\infty} x \left(7 - 4\frac{\sqrt{x}}{x} \right) = \lim_{x \rightarrow +\infty} x \left(7 - \frac{4}{\sqrt{x}} \right) = (+\infty)(7 - 0) = \boxed{+\infty}$$

7.10 5)

$$\lim_{x \rightarrow +\infty} (-2x + 3\sqrt{x}) = \lim_{x \rightarrow +\infty} x \left(-2 + \frac{3}{\sqrt{x}} \right) = (+\infty)(-2 + 0) = \boxed{-\infty}$$

7.10 6)

$$\lim_{x \rightarrow +\infty} (5x - 2\sqrt{x} + 1) = \lim_{x \rightarrow +\infty} x \left(5 - \frac{2}{\sqrt{x}} + \frac{1}{x} \right) = (+\infty)(5 - 0 + 0) = \boxed{+\infty}$$

7.10 7)

$$\lim_{x \rightarrow +\infty} (-4x + 9\sqrt{x} - 11) = \lim_{x \rightarrow +\infty} x \left(-4 + \frac{9}{\sqrt{x}} - \frac{11}{x} \right) = (+\infty)(-4 + 0 - 0) = \boxed{-\infty}$$

7.10 8)

$$\lim_{x \rightarrow +\infty} (2x^2 - x - 2\sqrt{x} - 8) = \lim_{x \rightarrow +\infty} x^2 \left(2 - \frac{1}{x} - \frac{2}{x\sqrt{x}} - \frac{8}{x^2} \right) = (+\infty)(2 - 0 - 0 - 0) = \boxed{+\infty}$$

7.10 9)

$$\lim_{x \rightarrow +\infty} \frac{\sqrt{x} - 10x}{5x + 2} = \lim_{x \rightarrow +\infty} \frac{\cancel{x} \left(\frac{1}{\sqrt{x}} - 10 \right)}{\cancel{x} \left(5 + \frac{2}{x} \right)} = \frac{0 - 10}{5 + 0} = \boxed{-2}$$