

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

7.1 1)

$$\alpha) \lim_{x \rightarrow +\infty} (x^3 - 3x^2 + x - 4) = \lim_{x \rightarrow +\infty} x^3 \left(1 - \frac{3}{x} + \frac{1}{x^2} - \frac{4}{x^3} \right) = (+\infty)(1 - 0 + 0 - 0) = \boxed{+\infty}$$

$$\beta) \lim_{x \rightarrow -\infty} (-2x^5 + x - 7) = \lim_{x \rightarrow -\infty} x^5 \left(-2 + \frac{1}{x^4} - \frac{7}{x^5} \right) = (-\infty)(-2 + 0 - 0) = \boxed{+\infty}$$

7.1 2)

$$\lim_{x \rightarrow +\infty} (2x^2 - 3x + 1) = \lim_{x \rightarrow +\infty} x^2 \left(2 - \frac{3}{x} + \frac{1}{x^2} \right) = (+\infty)(2 - 0 + 0) = \boxed{+\infty}$$

7.1 3)

$$\lim_{x \rightarrow -\infty} (4x^2 + 2x - 7) = \lim_{x \rightarrow -\infty} x^2 \left(4 + \frac{2}{x} - \frac{7}{x^2} \right) = (+\infty)(4 + 0 - 0) = \boxed{+\infty}$$

7.1 4)

$$\lim_{x \rightarrow -\infty} (2x^2 + 5x + 3) = \lim_{x \rightarrow -\infty} x^2 \left(2 + \frac{5}{x} + \frac{3}{x^2} \right) = (+\infty)(2 + 0 + 0) = \boxed{+\infty}$$

7.1 5)

$$\lim_{x \rightarrow -\infty} (-2x^3 - 2x^2 + 4x - 1) = \lim_{x \rightarrow -\infty} x^3 \left(-2 - \frac{2}{x} + \frac{4}{x^2} - \frac{1}{x^3} \right) = (-\infty)(-2 - 0 + 0 - 0) = \boxed{+\infty}$$

7.1 6)

$$\lim_{x \rightarrow -\infty} (-7x^3 - 8x + 1) = \lim_{x \rightarrow -\infty} x^3 \left(-7 - \frac{8}{x^2} + \frac{1}{x^3} \right) = (-\infty)(-7 - 0 + 0) = \boxed{+\infty}$$

7.1 7)

$$\lim_{x \rightarrow +\infty} (-3x^4 + 5x^2 + 1) = \lim_{x \rightarrow +\infty} x^4 \left(-3 + \frac{5}{x^2} + \frac{1}{x^4} \right) = (+\infty)(-3 + 0 + 0) = \boxed{-\infty}$$

7.1 8)

$$\lim_{x \rightarrow -\infty} (x^4 + 5x^3 + 1) = \lim_{x \rightarrow -\infty} x^4 \left(1 + \frac{5}{x} + \frac{1}{x^4} \right) = (-\infty)(1 + 0 + 0) = \boxed{+\infty}$$

7.1 9)

$$\begin{aligned} \lim_{x \rightarrow +\infty} (-x^5 + 3x^4 + 2x^2 + x - 3) &= \lim_{x \rightarrow +\infty} x^5 \left(-1 + \frac{3}{x} + \frac{2}{x^3} + \frac{1}{x^4} - \frac{3}{x^5} \right) = \\ &= (+\infty)(-1 + 0 + 0 + 0 - 0) = \boxed{-\infty} \end{aligned}$$

7.1 10)

$$\lim_{x \rightarrow -\infty} (x^5 + x + 1) = \lim_{x \rightarrow -\infty} x^5 \left(1 + \frac{1}{x^4} + \frac{1}{x^5} \right) = (-\infty)(1 + 0 + 0) = \boxed{-\infty}$$

7.1 11)

$$\lim_{x \rightarrow -\infty} (-5x^5 + 8x - 1) = \lim_{x \rightarrow -\infty} x^5 \left(-5 + \frac{8}{x^4} - \frac{1}{x^5} \right) = (-\infty)(-5 + 0 - 0) = \boxed{+\infty}$$

