

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

6.13 1)

$$\alpha) \lim_{x \rightarrow \frac{\pi}{2}} \frac{2x+1}{\eta\mu x - 1} = \lim_{x \rightarrow \frac{\pi}{2}} (2x+1) \cdot \lim_{x \rightarrow \frac{\pi}{2}} \frac{1}{\eta\mu x - 1} = \left(2 \cdot \frac{\pi}{2} + 1 \right) \cdot (-\infty) = \boxed{-\infty}$$

$$\beta) \lim_{x \rightarrow 0^+} \frac{x^2 + x + 1}{\sigma\upsilon\nu x} = \lim_{x \rightarrow 0^+} (x^2 + x + 1) \cdot \lim_{x \rightarrow 0^+} \frac{1}{\sigma\upsilon\nu x} = 1 \cdot (-\infty) = \boxed{-\infty}$$

$$\gamma) \lim_{x \rightarrow 0^-} \frac{3x-2}{\varepsilon\phi x} = \lim_{x \rightarrow 0^-} \frac{3x-2}{\eta\mu x} = \lim_{x \rightarrow 0^-} \frac{(3x-2)\sigma\upsilon\nu x}{\eta\mu x} =$$

$$= \lim_{x \rightarrow 0^-} [(3x-2)\sigma\upsilon\nu x] \cdot \lim_{x \rightarrow 0^-} \frac{1}{\eta\mu x} = [(3 \cdot 0 - 2) \cdot 1] \cdot (-\infty) = -2 \cdot (-\infty) = \boxed{+\infty}$$

6.13 2)

$$\lim_{x \rightarrow 0} \frac{2x+3}{1-\sigma\upsilon\nu x} = \lim_{x \rightarrow 0} (2x+3) \cdot \lim_{x \rightarrow 0} \frac{1}{1-\sigma\upsilon\nu x} \stackrel{\sigma\upsilon\nu x \leq 1 \Rightarrow 1-\sigma\upsilon\nu x \geq 0}{=} (2 \cdot 0 + 3) \cdot (+\infty) = \boxed{+\infty}$$

6.13 3)

$$\lim_{x \rightarrow 0} \frac{3x+1}{1-\sigma\upsilon\nu x} = \lim_{x \rightarrow 0} (3x+1) \cdot \lim_{x \rightarrow 0} \frac{1}{1-\sigma\upsilon\nu x} = (3 \cdot 0 + 1) \cdot (+\infty) = 1 \cdot (+\infty) = \boxed{+\infty}$$

6.13 4)

$$\lim_{x \rightarrow \frac{\pi}{2}^-} \frac{2x^2 - x}{\sigma\upsilon\nu x} = \lim_{x \rightarrow \frac{\pi}{2}^-} (2x^2 - x) \cdot \lim_{x \rightarrow \frac{\pi}{2}^-} \frac{1}{\sigma\upsilon\nu x} = \left(2 \cdot \frac{\pi^2}{4} - \frac{\pi}{2} \right) \cdot (+\infty) = \boxed{+\infty}$$

6.13 5)

$$\lim_{x \rightarrow 0} \frac{3x^2 - x + 2}{\sigma\upsilon\nu x - 1} = \lim_{x \rightarrow 0} (3x^2 - x + 2) \cdot \lim_{x \rightarrow 0} \frac{1}{\sigma\upsilon\nu x - 1} = (3 \cdot 0^2 - 0 + 2) \cdot (-\infty) = -\infty$$

6.13 6)

$$\lim_{x \rightarrow \frac{\pi}{2}} \frac{x^2 - 2x}{1 - \eta\mu x} = \lim_{x \rightarrow \frac{\pi}{2}} (x^2 - 2x) \cdot \lim_{x \rightarrow \frac{\pi}{2}} \frac{1}{1 - \eta\mu x} = \left(\frac{\pi^2}{4} - 2 \cdot \frac{\pi}{2} \right) \cdot (+\infty) =$$

$$= \frac{\pi^2 - 4\pi}{4} \cdot (+\infty) \stackrel{\pi^2 - 4\pi = \pi(\pi - 4) < 0}{=} \boxed{-\infty}$$

6.13 7)

$$\lim_{x \rightarrow 0^-} \frac{x^2 + x - 5}{\eta\mu x} = \lim_{x \rightarrow 0^-} (x^2 + x - 5) \cdot \lim_{x \rightarrow 0^-} \frac{1}{\eta\mu x} = (0^2 + 0 - 5) \cdot (-\infty) = \boxed{+\infty}$$

6.13 8)

$$\lim_{x \rightarrow \frac{\pi}{2}} (4x-1)\varepsilon\phi x = \lim_{x \rightarrow \frac{\pi}{2}} \frac{(4x-1)\eta\mu x}{\sigma\upsilon\nu x} = \lim_{x \rightarrow \frac{\pi}{2}} [(4x-1)\eta\mu x] \cdot \lim_{x \rightarrow \frac{\pi}{2}} \frac{1}{\sigma\upsilon\nu x} =$$

$$= \left[\left(4 \cdot \frac{\pi}{2} - 1 \right) \eta\mu \frac{\pi}{2} \right] \cdot (+\infty) = (2\pi - 1)(+\infty) = \boxed{+\infty}$$

6.13 9)

$$\lim_{x \rightarrow 0^+} (x^2 - 3) \sigma \varphi x = \lim_{x \rightarrow 0^+} \frac{(x^2 - 3) \sigma \nu x}{\eta \mu x} = \lim_{x \rightarrow 0^+} ((x^2 - 3) \sigma \nu x) \cdot \lim_{x \rightarrow 0^+} \frac{1}{\eta \mu x} =$$

$$(0^2 - 3) \cdot 1 \cdot (+\infty) = -3 \cdot (-\infty) = \boxed{-\infty}$$

6.13 10)

$$\lim_{x \rightarrow \frac{3\pi}{2}^+} \frac{6x - 1}{\sigma \varphi x} = \lim_{x \rightarrow \frac{3\pi}{2}^+} \frac{6x - 1}{\frac{\sigma \nu x}{\eta \mu x}} = \lim_{x \rightarrow \frac{3\pi}{2}^+} \frac{(6x - 1) \eta \mu x}{\sigma \nu x} = \lim_{x \rightarrow \frac{3\pi}{2}^+} [(6x - 1) \eta \mu x] \cdot \lim_{x \rightarrow \frac{3\pi}{2}^+} \frac{1}{\sigma \nu x} =$$

$$= \left(6 \frac{3\pi}{2} - 1 \right) (-1) \cdot (+\infty) = \boxed{-\infty}$$

6.13 11)

$$\lim_{x \rightarrow \pi^-} \frac{2x^2 - x - 1}{\varepsilon \varphi x} = \lim_{x \rightarrow \pi^-} \frac{2x^2 - x - 1}{\frac{\eta \mu x}{\sigma \nu x}} = \lim_{x \rightarrow \pi^-} \frac{(2x^2 - x - 1) \sigma \nu x}{\eta \mu x} =$$

$$= \lim_{x \rightarrow \pi^-} [(2x^2 - x - 1) \sigma \nu x] \cdot \lim_{x \rightarrow \pi^-} \frac{1}{\eta \mu x} = (2 \cdot \pi^2 - \pi - 1) (-1) \cdot (-\infty) = \boxed{-\infty}$$