

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

15.9 1)

$$\alpha) (e^x \cdot x^7 \cdot \sin x)' = (e^x)' x^7 \sin x + e^x (x^7)' \sin x + e^x x^7 (\sin x)' = \\ = e^x x^7 \sin x + 7e^x x^6 \sin x - e^x x^7 \eta \mu x$$

$$\beta) (x^4 \cdot 5^x \cdot \ln x \cdot \epsilon \phi x)' = \\ = (x^4)' 5^x \ln x \cdot \epsilon \phi x + x^4 (5^x)' \ln x \cdot \epsilon \phi x + x^4 \cdot 5^x (\ln x)' \epsilon \phi x + x^4 \cdot 5^x \ln x (\epsilon \phi x)' = \\ = 4x^3 \cdot 5^x \ln x \cdot \epsilon \phi x + x^4 \cdot 5^x \ln 5 \ln x \cdot \epsilon \phi x + x^3 5^x \epsilon \phi x + \frac{x^4 5^x \ln x}{\sin^2 x}$$

15.9 2)

$$(5^x)' \ln x \cdot \epsilon \phi x + 5^x (\ln x)' \epsilon \phi x + 5^x \ln x (\epsilon \phi x)' = 5^x \ln 5 \cdot \ln x \cdot \epsilon \phi x + \frac{5^x \cdot \epsilon \phi x}{x} + \frac{5^x \ln x}{\sin^2 x}$$

15.9 3)

$$(x^5)' \eta \mu x \cdot \sin x + x^5 (\eta \mu x)' \sin x + x^5 \eta \mu x (\sin x)' = 5x^4 \eta \mu x \cdot \sin x + x^5 \sin^2 x - x^5 \eta \mu^2 x$$

15.9 4)

$$\left(\frac{1}{x}\right)' \sin x \cdot \ln x + \frac{1}{x} (\sin x)' \ln x + \frac{1}{x} \sin x (\ln x)' = -\frac{\sin x \ln x}{x^2} - \frac{\eta \mu x \ln x}{x} + \frac{\sin x}{x^2}$$

15.9 5)

$$(4^x)' \sqrt{x} \cdot \sigma \phi x + 4^x (\sqrt{x})' \sigma \phi x + 4^x \sqrt{x} (\sigma \phi x)' = 4^x \ln 4 \cdot \sqrt{x} \cdot \sigma \phi x + \frac{4^x \sigma \phi x}{2\sqrt{x}} - \frac{4^x \sqrt{x}}{\eta \mu^2 x}$$

15.9 6)

$$(3^x)' x^6 \sin x + 3^x (x^6)' \sin x + 3^x x^6 (\sin x)' = 3^x \ln 3 \cdot x^6 \sin x + 6 \cdot 3^x x^5 \sin x - 3^x x^6 \eta \mu x$$

15.9 7)

$$\left(\frac{1}{x}\right)' \ln x \cdot \sigma \phi x + \frac{1}{x} (\ln x)' \sigma \phi x + \frac{1}{x} \ln x (\sigma \phi x)' = -\frac{\ln x \cdot \sigma \phi x}{x^2} + \frac{\sigma \phi x}{x^2} - \frac{\ln x}{x \eta \mu^2 x}$$

15.9 8)

$$(x-1)' (x-2)x^2 + (x-1)(x-2)' x^2 + (x-1)(x-2)(x^2)' = \\ = (x-2)x^2 + (x-1)x^2 + 2x(x-1)(x-2)$$

15.6 9)

$$(3x-2)' (x^2-8)(x^2-2x+7) + (3x+2)(x^2-8)' (x^2-2x+7) + (3x+2)(x^2-8)(x^2-2x+7)' = \\ = 3(x^2-8)(x^2-2x+7) + 2x(3x+2)(x^2-2x+7) + (3x+2)(x^2-8)(2x-2)$$

15.9 10)

$$(x)' (x^2+1)(x^3-2x) + x(x^2+1)' (x^3-2x) + x(x^2+1)(x^3-2x)' =$$

$$= (x^2 + 1)(x^3 - 2x) + 2x^2(x^3 - 2x) + x(x^2 + 1)(3x^2 - 2)$$

15.9 11)

$$\begin{aligned} & (e^x)' 3^x \eta \mu x \cdot \sigma \nu x + e^x (3^x)' \eta \mu x \cdot \sigma \nu x + e^x \cdot 3^x (\eta \mu x)' \sigma \nu x + e^x \cdot 3^x \eta \mu x (\sigma \nu x)' \\ & = e^x \cdot 3^x \cdot \eta \mu x \cdot \sigma \nu x + e^x \cdot 3^x \ln 3 \cdot \eta \mu x \cdot \sigma \nu x + e^x \cdot 3^x \sigma \nu^2 x - e^x \cdot 3^x \cdot \eta \mu^2 x \end{aligned}$$

15.9 12)

$$\begin{aligned} & (2x - 1)' (5\eta \mu x + x^2) (\ln x + 3e^x) \sigma \varphi x + (2x - 1) (5\eta \mu x + x^2)' (\ln x + 3e^x) \sigma \varphi x + \\ & + (2x - 1) (5\eta \mu x + x^2) (\ln x + 3e^x)' \sigma \varphi x + (2x - 1) (5\eta \mu x + x^2) (\ln x + 3e^x) (\sigma \varphi x)' = \\ & = 2 (5\eta \mu x + x^2) (\ln x + 3e^x) \sigma \varphi x + (2x - 1) (5\sigma \nu x + 2x) (\ln x + 3e^x) \sigma \varphi x + \\ & + (2x - 1) (5\eta \mu x + x^2) \left(\frac{1}{x} + 3e^x \right) \sigma \varphi x - \frac{(2x - 1) (5\eta \mu x + x^2) (\ln x + 3e^x)}{\eta \mu^2 x} \end{aligned}$$

15.9 13)

$$\begin{aligned} & \left(\frac{1}{x} \right)' \cdot 4^x \cdot \eta \mu x \cdot \ln x + \frac{1}{x} \cdot (4^x)' \cdot \eta \mu x \cdot \ln x + \frac{1}{x} \cdot 4^x \cdot (\eta \mu x)' \cdot \ln x + \frac{1}{x} \cdot 4^x \cdot \eta \mu x \cdot (\ln x)' = \\ & = -\frac{4^x \cdot \eta \mu x \cdot \ln x}{x^2} + \frac{4^x \ln 4 \cdot \eta \mu x \cdot \ln x}{x} + \frac{4^x \cdot \sigma \nu x \cdot \ln x}{x} + \frac{4^x \cdot \eta \mu x}{x^2} \end{aligned}$$