

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

15.7 1)

$$\alpha) (x)' \ln x + x (\ln x)' = 1 \cdot \ln x + x \cdot \frac{1}{x} = \ln x + 1$$

$$\beta) (x^2)' \eta\mu x + x^2 (\eta\mu x)' = 2x \cdot \eta\mu x + x^2 \sigma\upsilon\nu x$$

$$\gamma) (e^x)' \sqrt{x} + e^x (\sqrt{x})' = e^x \sqrt{x} + e^x \frac{1}{2\sqrt{x}}$$

$$\delta) (x^2 - 2x)' \sigma\varphi x + (x^2 - 2x) (\sigma\varphi x)' = (2x - 2) \sigma\varphi x - \frac{x^2 - 2x}{\eta\mu^2 x}$$

15.7 2)

$$\left(\frac{1}{x}\right)' \ln x + \frac{1}{x} (\ln x)' = -\frac{1}{x^2} \ln x + \frac{1}{x} \cdot \frac{1}{x} = \frac{1 - \ln x}{x^2}$$

15.7 3)

$$\left(\frac{1}{x}\right)' 6^x + \frac{1}{x} (6^x)' = -\frac{1}{x^2} 6^x + \frac{1}{x} 6^x \ln 6$$

15.7 4)

$$(\sqrt{x})' \frac{1}{x} + \sqrt{x} \left(\frac{1}{x}\right)' = \frac{1}{2\sqrt{x}} \frac{1}{x} + \sqrt{x} \left(-\frac{1}{x^2}\right) = \frac{2}{2x\sqrt{x}} - \frac{\sqrt{x}}{x^2}$$

15.7 5)

$$(e^x)' \sigma\upsilon\nu x + e^x (\sigma\upsilon\nu x)' = e^x \sigma\upsilon\nu x - e^x \eta\mu x$$

15.7 6)

$$(4x^3)' \varepsilon\varphi x + 4x^3 (\varepsilon\varphi x)' = 12x^2 \varepsilon\varphi x + \frac{4x^3}{\sigma\upsilon\nu^2 x}$$

15.7 7)

$$(\eta\mu x)' \sigma\upsilon\nu x + \eta\mu x (\sigma\upsilon\nu x)' = \sigma\upsilon\nu x \cdot \sigma\upsilon\nu x + \eta\mu x (-\eta\mu x) = \sigma\upsilon\nu^2 x - \eta\mu^2 x$$

15.7 8)

$$(e^x)' \eta\mu x + e^x (\eta\mu x)' = e^x \eta\mu x + e^x \sigma\upsilon\nu x$$

15.7 9)

$$\left(\frac{1}{x}\right)' \sigma\varphi x + \frac{1}{x} (\sigma\varphi x)' = -\frac{1}{x^2} \sigma\varphi x - \frac{1}{x \cdot \eta\mu^2 x}$$

15.7 10)

$$(4^x)' \eta\mu x + 4^x (\eta\mu x)' = 4^x \ln 4 \cdot \eta\mu x + 4^x \sigma\upsilon\nu x$$

15.7 11)

$$\left(\frac{1}{x}\right)' \varepsilon \varphi x + \frac{1}{x} (\varepsilon \varphi x)' = -\frac{1}{x^2} \varepsilon \varphi x + \frac{1}{x \sigma \nu v^2 x}$$

15.7 12)

$$(e^x)' \sigma \varphi x + e^x (\sigma \varphi x)' = e^x \sigma \varphi x - \frac{e^x}{\eta \mu^2 x}$$

15.7 13)

$$(\sqrt{x})' \sigma \varphi x + \sqrt{x} (\sigma \varphi x)' = \frac{1}{2\sqrt{x}} \sigma \varphi x - \frac{\sqrt{x}}{\eta \mu^2 x}$$

15.7 14)

$$(\sqrt{x})' 3^x + \sqrt{x} (3^x)' = \frac{1}{2\sqrt{x}} 3^x + \sqrt{x} \cdot 3^x \ln 3$$

15.7 15)

$$(x^2)' \sqrt{x} + x^2 (\sqrt{x})' = 2x \sqrt{x} + \frac{x^2}{2\sqrt{x}}$$

15.7 16)

$$(3x^2 - 2x)' \frac{1}{x} + (3x^2 - 2x) \left(\frac{1}{x}\right)' = \frac{6x - 2}{x} - \frac{3x^2 - 2x}{x^2}$$

15.7 17)

$$\left(\frac{1}{x}\right)' \eta \mu x + \frac{1}{x} (\eta \mu x)' = -\frac{1}{x^2} \eta \mu x + \frac{\sigma \nu v x}{x}$$

15.7 18)

$$(\varepsilon \varphi x)' \ln x + \varepsilon \varphi x (\ln x)' = \frac{\ln x}{\sigma \nu v^2 x} + \frac{\varepsilon \varphi x}{x}$$

15.7 19)

$$(x^3 - x + 5)' \sigma \varphi x + (x^3 - x + 5) (\sigma \varphi x)' = (3x^2 - 1) \sigma \varphi x - \frac{x^3 - x + 5}{\eta \mu^2 x}$$

15.7 20)

$$20) \quad (\sigma \varphi x \cdot \ln x)' = (\sigma \varphi x)' \cdot \ln x + \sigma \varphi x \cdot (\ln x)' = -\frac{\ln x}{\eta \mu^2 x} + \frac{\sigma \varphi x}{x}$$

15.7 21)

$$21) \quad (\sigma \nu v x \cdot \sigma \varphi x)' = (\sigma \nu v x)' \cdot \sigma \varphi x + \sigma \nu v x \cdot (\sigma \varphi x)' = -\eta \mu x \cdot \sigma \varphi x - \frac{\sigma \nu v x}{\eta \mu^2 x}$$

15.7 22)

$$22) \quad \left(\frac{1}{x} \cdot e^x\right)' = \left(\frac{1}{x}\right)' \cdot e^x + \frac{1}{x} \cdot (e^x)' = -\frac{e^x}{x^2} + \frac{e^x}{x}$$

15.7 23)

$$23) \quad (e^x \cdot 7^x)' = (e^x)' \cdot 7^x + e^x \cdot (7^x)' = e^x \cdot 7^x + e^x \cdot 7^x \ln 7$$

15.7 24)

$$24) \quad \left(x^4 \cdot \eta\mu x\right)' = \left(x^4\right)' \cdot \eta\mu x + x^4 \cdot (\eta\mu x)' = 4x^3 \eta\mu x + x^4 \sigma\upsilon\nu x$$

15.7 25)

$$25) \quad \left(x^3 \cdot 2^x\right)' = \left(x^3\right)' \cdot 2^x + x^3 \cdot \left(2^x\right)' = 3x^2 \cdot 2^x + x^3 \cdot 2^x \ln 2$$

15.7 26)

$$26) \quad \left(\eta\mu x \cdot \ln x\right)' = (\eta\mu x)' \cdot \ln x + \eta\mu x \cdot (\ln x)' = \sigma\upsilon\nu x \cdot \ln x + \frac{\eta\mu x}{x}$$

15.7 27)

$$27) \quad \left(\sqrt{x} \cdot \varepsilon\varphi x\right)' = \left(\sqrt{x}\right)' \cdot \varepsilon\varphi x + \sqrt{x} \cdot (\varepsilon\varphi x)' = \frac{\varepsilon\varphi x}{2\sqrt{x}} + \frac{\sqrt{x}}{\sigma\upsilon\nu^2 x}$$

15.7 28)

$$28) \quad \left(\frac{1}{x} \cdot \sigma\upsilon\nu x\right)' = \left(\frac{1}{x}\right)' \cdot \sigma\upsilon\nu x + \frac{1}{x} \cdot (\sigma\upsilon\nu x)' = -\frac{\sigma\upsilon\nu x}{x^2} - \frac{\eta\mu x}{x}$$