

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

15.25 1)

a) $\left[\sqrt{\varepsilon\varphi(2x^4 - x)} \right]' = \frac{1}{2\sqrt{\varepsilon\varphi(2x^4 - x)}} \left[\varepsilon\varphi(2x^4 - x) \right]' =$

$$= \frac{1}{2\sqrt{\varepsilon\varphi(2x^4 - x)}} \frac{1}{\sigma\psi v^2(2x^4 - x)} (2x^4 - x)' = \frac{1}{2\sqrt{\varepsilon\varphi(2x^4 - x)}} \frac{8x^3 - 1}{\sigma\psi v^2(2x^4 - x)}$$

b) $\left[\sigma\psi v^5(\eta\mu x) \right]' = 5\sigma\psi v^4(\eta\mu x) \cdot \left[\sigma\psi v(\eta\mu x) \right]' =$

$$= 5\sigma\psi v^4(\eta\mu x) \cdot [-\eta\mu(\eta\mu x)] \cdot (\eta\mu x)' = -5\sigma\psi v^4(\eta\mu x) \cdot \eta\mu(\eta\mu x) \cdot (\sigma\psi v x)$$

15.25 2)

$$\left[\sqrt{\eta\mu(x^2 + 3x)} \right]' = \frac{1}{2\sqrt{\eta\mu(x^2 + 3x)}} \left[\eta\mu(x^2 + 3x) \right]' =$$

$$= \frac{1}{2\sqrt{\eta\mu(x^2 + 3x)}} \sigma\psi v(x^2 + 3x) \cdot (x^2 + 3x)' = \frac{1}{2\sqrt{\eta\mu(x^2 + 3x)}} \sigma\psi v(x^2 + 3x) \cdot (2x + 3)$$

15.25 3)

$$\left[\sqrt{\sigma\psi v(\ln x)} \right]' = \frac{1}{2\sqrt{\sigma\psi v(\ln x)}} \left[\sigma\psi v(\ln x) \right]' = \frac{1}{2\sqrt{\sigma\psi v(\ln x)}} [-\eta\mu(\ln x)] \cdot (\ln x)' =$$

$$= \frac{-\eta\mu(\ln x)}{2x\sqrt{\sigma\psi v(\ln x)}}$$

15.25 4)

$$\left[\sqrt{\ln(\sigma\varphi x)} \right]' = \frac{1}{2\sqrt{\ln(\sigma\varphi x)}} \left[\ln(\sigma\varphi x) \right]' = \frac{1}{2\sqrt{\ln(\sigma\varphi x)}} \frac{1}{\sigma\varphi x} (\sigma\varphi x)' =$$

$$= \frac{1}{2\sqrt{\ln(\sigma\varphi x)}} \frac{1}{\sigma\varphi x} \frac{-1}{\eta\mu^2 x}$$

15.25 5)

$$\left[\sigma\psi v(\ln(\varepsilon\varphi x)) \right]' = -\eta\mu(\ln(\varepsilon\varphi x)) \cdot \left[\ln(\varepsilon\varphi x) \right]' = -\eta\mu(\ln(\varepsilon\varphi x)) \cdot \frac{1}{\varepsilon\varphi x} (\varepsilon\varphi x)' =$$

$$= -\eta\mu(\ln(\varepsilon\varphi x)) \cdot \frac{1}{\varepsilon\varphi x} \frac{1}{\sigma\psi v^2 x}$$

15.25 6)

$$\left[\sigma\varphi(\ln(\eta\mu x)) \right]' = -\frac{1}{\eta\mu^2(\ln(\eta\mu x))} (\ln(\eta\mu x))' = -\frac{1}{\eta\mu^2(\ln(\eta\mu x))} \frac{1}{\eta\mu x} (\eta\mu x)' =$$

$$= -\frac{1}{\eta\mu^2(\ln(\eta\mu x))} \frac{1}{\eta\mu x} \sigma\psi v x$$

15.25 7)

$$\left[\varepsilon\varphi(\ln\sqrt{x}) \right]' = \frac{1}{\sigma\psi v^2(\ln\sqrt{x})} \cdot (\ln\sqrt{x})' = \frac{1}{\sigma\psi v^2(\ln\sqrt{x})} \cdot \frac{1}{\sqrt{x}} (\sqrt{x})' =$$

$$= \frac{1}{\sigma\psi v^2(\ln\sqrt{x})} \cdot \frac{1}{\sqrt{x}} \frac{1}{2\sqrt{x}} = \frac{1}{2x\sigma\psi v^2(\ln\sqrt{x})}$$

$$\begin{aligned} \left[\sigma v v \left(\sqrt{e^x + x} \right) \right]' &= -\eta \mu \left(\sqrt{e^x + x} \right) \cdot \left(\sqrt{e^x + x} \right)' = \\ &= -\eta \mu \left(\sqrt{e^x + x} \right) \cdot \frac{1}{2\sqrt{e^x + x}} (e^x + x)' = -\eta \mu \left(\sqrt{e^x + x} \right) \cdot \frac{1}{2\sqrt{e^x + x}} (e^x + 1) \end{aligned}$$

15.25 9)

$$\begin{aligned} \left[\sigma v v \left(\sqrt{3^x + x} \right) \right]' &= -\eta \mu \left(\sqrt{3^x + x} \right) \cdot \left(\sqrt{3^x + x} \right)' = \\ &= -\eta \mu \left(\sqrt{3^x + x} \right) \cdot \frac{1}{2\sqrt{3^x + x}} (3^x + x)' = -\eta \mu \left(\sqrt{3^x + x} \right) \cdot \frac{1}{2\sqrt{3^x + x}} (3^x \ln 3 + 1) \end{aligned}$$

15.25 10)

$$\begin{aligned} \left(\ln \sqrt{5e^x + x^2} \right)' &= \frac{1}{\sqrt{5e^x + x^2}} \cdot \left(\sqrt{5e^x + x^2} \right)' = \frac{1}{\sqrt{5e^x + x^2}} \cdot \frac{1}{2\sqrt{5e^x + x^2}} (5e^x + x^2)' = \\ &= \frac{1}{\sqrt{5e^x + x^2}} \cdot \frac{1}{2\sqrt{5e^x + x^2}} (5e^x + 2x) \end{aligned}$$

15.25 11)

$$\begin{aligned} \ln \left[\varepsilon \varphi \left(5^x + x^4 \right) \right]' &= \frac{1}{\varepsilon \varphi \left(5^x + x^4 \right)} \left[\varepsilon \varphi \left(5^x + x^4 \right) \right]' \\ &= \frac{1}{\varepsilon \varphi \left(5^x + x^4 \right)} \frac{1}{\sigma v v^2 \left(5^x + x^4 \right)} (5^x + x^4)' = \frac{1}{\varepsilon \varphi \left(5^x + x^4 \right)} \frac{1}{\sigma v v^2 \left(5^x + x^4 \right)} (5^x \ln 5 + 4x^3) = \end{aligned}$$

15.25 12)

$$\begin{aligned} \left[\eta \mu \left(\sigma v v (\varepsilon \varphi x) \right) \right]' &= \sigma v v (\sigma v v (\varepsilon \varphi x)) \cdot \left[\sigma v v (\varepsilon \varphi x) \right]' = \\ &= \sigma v v (\sigma v v (\varepsilon \varphi x)) \cdot \left[-\eta \mu (\varepsilon \varphi x) \right] (\varepsilon \varphi x)' = -\sigma v v (\sigma v v (\varepsilon \varphi x)) \cdot \eta \mu (\varepsilon \varphi x) \frac{1}{\sigma v v^2 x} \end{aligned}$$

15.25 13)

$$\begin{aligned} \left[\eta \mu \left(\eta \mu (\eta \mu x) \right) \right]' &= \sigma v v (\eta \mu (\eta \mu x)) \cdot \left[\eta \mu (\eta \mu x) \right]' = \\ &= \sigma v v (\eta \mu (\eta \mu x)) \cdot \sigma v v (\eta \mu x) (\eta \mu x)' = \sigma v v (\eta \mu (\eta \mu x)) \cdot \sigma v v (\eta \mu x) \sigma v v x = \end{aligned}$$

15.25 14)

$$\begin{aligned} \left[e^{\eta \mu (\sigma v v x)} \right]' &= e^{\eta \mu (\sigma v v x)} \left[\eta \mu (\sigma v v x) \right]' = e^{\eta \mu (\sigma v v x)} \sigma v v (\sigma v v x) \cdot (\sigma v v x)' = \\ &= e^{\eta \mu (\sigma v v x)} \sigma v v (\sigma v v x) \cdot (-\eta \mu x) = -e^{\eta \mu (\sigma v v x)} \sigma v v (\sigma v v x) \cdot \eta \mu x \end{aligned}$$

15.25 15)

$$\left(\frac{1}{\sqrt{\ln x}} \right)' = -\frac{1}{\sqrt{\ln x}^2} (\sqrt{\ln x})' = -\frac{1}{\ln x} \frac{1}{2\sqrt{\ln x}} (\ln x)' = -\frac{1}{\ln x} \frac{1}{2\sqrt{\ln x}} \frac{1}{x}$$

15.25 16)

$$\left[4^{\ln(\varepsilon \varphi x)} \right]' = 4^{\ln(\varepsilon \varphi x)} \ln 4 \left[\ln(\varepsilon \varphi x) \right]' = 4^{\ln(\varepsilon \varphi x)} \ln 4 \frac{1}{\varepsilon \varphi x} (\varepsilon \varphi x)' = 4^{\ln(\varepsilon \varphi x)} \ln 4 \frac{1}{\varepsilon \varphi x} \frac{1}{\sigma v v^2 x}$$

15.25 17)

$$\left(7^{3^{\sigma v v x}} \right)' = 7^{3^{\sigma v v x}} \ln 7 \cdot \left(3^{\sigma v v x} \right)' = 7^{3^{\sigma v v x}} \ln 7 \cdot 3^{\sigma v v x} \ln 3 \cdot (\sigma v v x)' = 7^{3^{\sigma v v x}} \ln 7 \cdot 3^{\sigma v v x} \ln 3 \cdot (-\eta \mu x) =$$

$$= -7^{3^{\sigma v v x}} \ln 7 \cdot 3^{\sigma v v x} \ln 3 \cdot \eta \mu x$$

15.25 18)

$$\begin{aligned} [\eta \mu (\sigma v v 2x)]' &= \sigma v v (\sigma v v 2x) \cdot (\sigma v v 2x)' = \sigma v v (\sigma v v 2x) \cdot (-\eta \mu 2x) (2x)' = \\ &= -\sigma v v (\sigma v v 2x) \cdot \eta \mu 2x \cdot 2 \end{aligned}$$

15.25 19)

$$\left(\sqrt{2^{3x}}\right)' = \frac{1}{2\sqrt{2^{3x}}} (2^{3x})' = \frac{1}{2\sqrt{2^{3x}}} 2^{3x} \cdot \ln 2 \cdot (3x)' = \frac{1}{2\sqrt{2^{3x}}} 2^{3x} \cdot \ln 2 \cdot 3$$

15.25 20)

$$(3^{\eta \mu 3x})' = 3^{\eta \mu 3x} \ln 3 \cdot (\eta \mu 3x)' = 3^{\eta \mu 3x} \ln 3 \cdot \sigma v v 3x \cdot (3x)' = 3^{\eta \mu 3x} \ln 3 \cdot \sigma v v 3x \cdot 3$$

15.25 21)

$$\begin{aligned} \left[\ln(\sqrt{x^2 + x + 3})\right]' &= \frac{1}{\sqrt{x^2 + x + 3}} (\sqrt{x^2 + x + 3})' = \\ &= \frac{1}{\sqrt{x^2 + x + 3}} \frac{1}{2\sqrt{x^2 + x + 3}} (x^2 + x + 3)' = \frac{1}{2\sqrt{x^2 + x + 3}} (2x + 1) = \frac{2x + 1}{2(x^2 + x + 3)} \end{aligned}$$

15.25 22)

$$\begin{aligned} \left[e^{\eta \mu (x^2 - x + 1)}\right]' &= e^{\eta \mu (x^2 - x + 1)} \left[\eta \mu (x^2 - x + 1)\right]' = e^{\eta \mu (x^2 - x + 1)} \sigma v v (x^2 - x + 1) \cdot (x^2 - x + 1)' = \\ &= e^{\eta \mu (x^2 - x + 1)} \sigma v v (x^2 - x + 1) \cdot (2x - 1) \end{aligned}$$

15.25 23)

$$\begin{aligned} \left[\eta \mu (\ln(\sqrt{x} - 1))\right]' &= \sigma v v (\ln(\sqrt{x} - 1)) \left[\ln(\sqrt{x} - 1)\right]' = \\ &= \sigma v v (\ln(\sqrt{x} - 1)) \frac{1}{\sqrt{x} - 1} (\sqrt{x} - 1)' = \sigma v v (\ln(\sqrt{x} - 1)) \frac{1}{\sqrt{x} - 1} \frac{1}{2\sqrt{x}} \end{aligned}$$

15.25 24)

$$\begin{aligned} \left(\sqrt{2\eta \mu 4x}\right)' &= \frac{1}{2\sqrt{2\eta \mu 4x}} \cdot (2\eta \mu 4x)' = \frac{1}{2\sqrt{2\eta \mu 4x}} \cdot (\cancel{2} \sigma v v 4x) \cdot (4x)' = \\ &= \frac{1}{\sqrt{2\eta \mu 4x}} \cdot \sigma v v 4x \cdot 4 \end{aligned}$$

15.25 25)

$$\begin{aligned} \left(\frac{1}{\sigma v v^2(\ln x)}\right)' &= -\frac{1}{\sigma v v^4(\ln x)} [\sigma v v^2(\ln x)]' = \\ &= -\frac{1}{\sigma v v^4(\ln x)} 2\sigma v v(\ln x) [\sigma v v(\ln x)]' = -\frac{2\sigma v v(\ln x)}{\sigma v v^4(\ln x)} [-\eta \mu(\ln x)] \cdot (\ln x)' = \\ &= \frac{2\sigma v v(\ln x) \eta \mu(\ln x)}{x \sigma v v^4(\ln x)} \end{aligned}$$