

Γ ΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

15.23 1)

$$\alpha) \left[\eta\mu(x^2 - \ln x) \right]' = \sigma\upsilon\nu(x^2 - \ln x) \cdot (x^2 - \ln x)' = \sigma\upsilon\nu(x^2 - \ln x) \cdot \left(2x - \frac{1}{x} \right)$$

$$\beta) \left(9^{3^x + 7e^x} \right)' = 9^{3^x + 7e^x} \cdot (3^x + 7e^x)' = 9^{3^x + 7e^x} \cdot (3^x \ln 3 + 7e^x) \ln 9$$

15.23 2)

$$\left(e^{x^5 - \sigma\varphi x} \right)' = e^{x^5 - \sigma\varphi x} \cdot (x^5 - \sigma\varphi x)' = e^{x^5 - \sigma\varphi x} \cdot \left(5x^4 + \frac{1}{\eta\mu^2 x} \right)$$

15.23 3)

$$\begin{aligned} \left[(\sigma\upsilon\nu x - 2 \ln x)^4 \right]' &= 4(\sigma\upsilon\nu x - 2 \ln x)^3 (\sigma\upsilon\nu x - 2 \ln x)' = \\ &= 4(\sigma\upsilon\nu x - 2 \ln x)^3 \left(-\eta\mu x - \frac{2}{x} \right) \end{aligned}$$

15.23 4)

$$\left(4^{\sqrt{x} + 2\eta\mu x} \right)' = 4^{\sqrt{x} + 2\eta\mu x} \left(\sqrt{x} + 2\eta\mu x \right)' = 4^{\sqrt{x} + 2\eta\mu x} \left(\frac{1}{2\sqrt{x}} + 2\sigma\upsilon\nu x \right)$$

15.23 5)

$$\left(\sqrt{x^3 + 3^x} \right)' = \frac{1}{2\sqrt{x^3 + 3^x}} \cdot (x^3 + 3^x)' = \frac{1}{2\sqrt{x^3 + 3^x}} \cdot (3x^2 + 3^x \ln 3)$$

15.23 6)

$$\left[\ln \left(\frac{1}{x} + 4\sqrt{x} \right) \right]' = \frac{1}{\frac{1}{x} + 4\sqrt{x}} \cdot \left(\frac{1}{x} + 4\sqrt{x} \right)' = \frac{1}{\frac{1}{x} + 4\sqrt{x}} \cdot \left(-\frac{1}{x^2} + 2\frac{1}{\sqrt{x}} \right)$$

15.23 7)

$$\left[(x^3 - \varepsilon\varphi x)^2 \right]' = 2(x^3 - \varepsilon\varphi x) \cdot (x^3 - \varepsilon\varphi x)' = 2(x^3 - \varepsilon\varphi x) \cdot \left(3x^2 - \frac{1}{\sigma\upsilon\nu^2 x} \right)$$

15.23 8)

$$\left[\ln \left(\frac{1}{x} + e^x \right) \right]' = \frac{1}{\frac{1}{x} + e^x} \cdot \left(\frac{1}{x} + e^x \right)' = \frac{1}{\frac{1}{x} + e^x} \cdot \left(-\frac{1}{x^2} + e^x \right)$$

15.23 9)

$$\left(6^{\frac{1}{x} - \varepsilon\varphi x} \right)' = 6^{\frac{1}{x} - \varepsilon\varphi x} \cdot \ln 6 \cdot \left(\frac{1}{x} - \varepsilon\varphi x \right)' = 6^{\frac{1}{x} - \varepsilon\varphi x} \cdot \left(-\frac{1}{x^2} - \frac{1}{\sigma\upsilon\nu^2 x} \right) \cdot \ln 6$$

15.23 10)

$$\left(\frac{1}{3x^2 + 2x} \right)' = -\frac{1}{(3x^2 + 2x)^2} \cdot (3x^2 + 2x)' = -\frac{1}{(3x^2 + 2x)^2} \cdot (6x + 2)$$

15.23 11)

$$\left[\eta\mu(5^x - e^x) \right]' = \sigma\upsilon\nu(5^x - e^x) \cdot (5^x - e^x)' = \sigma\upsilon\nu(5^x - e^x) \cdot (5^x \ln 5 - e^x)$$

15.23 12)

$$\left[\ln(2^x - 5^x) \right]' = \frac{1}{2^x - 5^x} \cdot (2^x \ln 2 - 5^x \ln 5)$$

15.23 13)

$$\left[\sigma\varphi(x^3 - 3\sqrt{x}) \right]' = -\frac{1}{\eta\mu^2(x^3 - 3\sqrt{x})} \cdot (x^3 - 3\sqrt{x})' = -\frac{3x^2 - \frac{3}{2\sqrt{x}}}{\eta\mu^2(x^3 - 3\sqrt{x})}$$

15.23 14)

$$\left(\sqrt{x^2 + x - 1} \right)' = \frac{1}{2\sqrt{x^2 + x - 1}} \cdot (x^2 + x - 1)' = \frac{1}{2\sqrt{x^2 + x - 1}} \cdot (2x + 1)$$

15.23 15)

$$\left[\sigma\varphi\left(\frac{1}{x} - 3^x\right) \right]' = -\frac{1}{\eta\mu^2\left(\frac{1}{x} - 3^x\right)} \left(\frac{1}{x} - 3^x\right)' = -\frac{1}{\eta\mu^2\left(\frac{1}{x} - 3^x\right)} \left(-\frac{1}{x} - 3^x \ln 3\right)$$

15.23 16)

$$\left(e^{x^3 + \varepsilon\varphi x} \right)' = \left(e^{x^3 + \varepsilon\varphi x} \right) (x^3 + \varepsilon\varphi x)' = \left(e^{x^3 + \varepsilon\varphi x} \right) \left(3x^2 + \frac{1}{\sigma\nu^2 x} \right)$$

15.23 17)

$$(\sigma\varphi^9 x)' = 9\sigma\varphi^8 x \cdot (\sigma\varphi x)' = 9\sigma\varphi^8 x \cdot \left(-\frac{1}{\eta\mu^2 x} \right) = -\frac{9\sigma\varphi^8 x}{\eta\mu^2 x}$$

15.23 18)

$$\left(e^{2-e^x} \right)' = e^{2-e^x} (2 - e^x)' = e^{2-e^x} (-e^x) = -e^{2+x-e^x}$$

15.23 19)

$$\begin{aligned} \left(14^{\frac{1}{x} + 2\sqrt{x}} \right)' &= 14^{\frac{1}{x} + 2\sqrt{x}} \ln 14 \cdot \left(\frac{1}{x} + 2\sqrt{x} \right)' = 14^{\frac{1}{x} + 2\sqrt{x}} \ln 14 \cdot \left(-\frac{1}{x^2} + \frac{1}{\cancel{2}\sqrt{x}} \right) = \\ &= 14^{\frac{1}{x} + 2\sqrt{x}} \ln 14 \cdot \left(-\frac{1}{x^2} + \frac{1}{\sqrt{x}} \right) \end{aligned}$$

15.23 20)

$$\left[\eta\mu(e^x + \ln x) \right]' = \sigma\nu(e^x + \ln x) \cdot (e^x + \ln x)' = \sigma\nu(e^x + \ln x) \cdot \left(e^x + \frac{1}{x} \right)$$

15.23 21)

$$\left(\sqrt{\frac{1}{x} + 4\sigma\nu x} \right)' = \frac{1}{2\sqrt{\frac{1}{x} + 4\sigma\nu x}} \left(\frac{1}{x} + 4\sigma\nu x \right)' = \frac{1}{2\sqrt{\frac{1}{x} + 4\sigma\nu x}} \left(-\frac{1}{x} - 4\eta\mu x \right)$$

15.23 22)

$$\left(e^{x^2 - 2^x} \right)' = e^{x^2 - 2^x} \cdot (x^2 - 2^x)' = e^{x^2 - 2^x} \cdot (2x - 2^x \ln 2)$$

15.23 23)

$$\left[\varepsilon\varphi(e^x - 3\sigma\nu x) \right]' = \frac{1}{\sigma\nu^2(e^x - 3\sigma\nu x)} \cdot (e^x - 3\sigma\nu x)' = \frac{e^x + 3\eta\mu x}{\sigma\nu^2(e^x - 3\sigma\nu x)}$$

15.23 24)

$$\left[\sigma \nu \left(x + \varepsilon \varphi x \right) \right]' = -\eta \mu \left(x + \varepsilon \varphi x \right) \cdot \left(x + \varepsilon \varphi x \right)' = -\eta \mu \left(x + \varepsilon \varphi x \right) \cdot \left(1 + \frac{1}{\sigma \nu^2 x} \right)$$

15.23 25)

$$\begin{aligned} \left[\eta \mu \left(5^x - 6 \sigma \nu x \right) \right]' &= \sigma \nu \left(5^x - 6 \sigma \nu x \right) \cdot \left(5^x - 6 \sigma \nu x \right)' = \\ &= \sigma \nu \left(5^x - 6 \sigma \nu x \right) \cdot \left(5^x \ln 5 + 6 \eta \mu x \right) \end{aligned}$$

15.23 26)

$$\left[\ln \left(x^4 - 3 \sqrt{x} \right) \right]' = \frac{1}{x^4 - 3 \sqrt{x}} \left(x^4 - 3 \sqrt{x} \right)' = \frac{1}{x^4 - 3 \sqrt{x}} \left(4x^3 - 3 \frac{1}{2 \sqrt{x}} \right)$$