

ΓΛΥΚΕΙΟΥ ΜΕΡΟΣ Α

14.7 1)

$$f(3+h) = h^2 + h - 1 \xrightarrow{h=0} f(3+0) = 0^2 + 0 - 1 \Rightarrow [f(3) = -1]$$

Ακόμη

$$[f'(3)] = \lim_{h \rightarrow 0} \frac{f(3+h) - f(3)}{h} \xrightarrow{f(3) = -1} \lim_{h \rightarrow 0} \frac{h^2 + h - 1 - (-1)}{h} = \lim_{h \rightarrow 0} \frac{h(h+1)}{h} = \lim_{h \rightarrow 0} h + 1 = 0 + 1 = [1]$$

$$\text{Άρα } [f(3) + f'(3)] = -1 + 1 = [0]$$

14.7 2)

$$\alpha) \quad f(1+h) = 2h^2 - h + 2 \xrightarrow{h=0} f(1+0) = 2 \cdot 0^2 - 0 + 2 \Rightarrow [f(1) = 2]$$

$$\beta) \quad [f'(1)] = \lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h} \xrightarrow{f(1) = 2} \lim_{h \rightarrow 0} \frac{2h^2 - h + 2 - 2}{h} = \\ = \lim_{h \rightarrow 0} \frac{h(2h-1)}{h} = 0 - 1 = [-1]$$

14.7 3)

$$\alpha) \quad f(2+h) = h^2 - 2h - 3 \xrightarrow{h=0} f(2+0) = 0^2 - 2 \cdot 0 - 3 \Rightarrow [f(2) = -3]$$

$$\beta) \quad [f'(2)] = \lim_{h \rightarrow 0} \frac{f(2+h) - f(2)}{h} \xrightarrow{f(2) = -3} \lim_{h \rightarrow 0} \frac{h^2 - 2h - 3 + 3}{h} = \\ = \lim_{h \rightarrow 0} \frac{h(h-2)}{h} = 0 - 2 = [-2]$$

14.7 4)

$$f(-5+h) = \frac{1-h}{2} + h^2 - h^3 \xrightarrow{h=0} f(-5+0) = \frac{1-0}{2} + 0^2 - 0^3 \Rightarrow [f(-5) = \frac{1}{2}]$$

Ακόμη

$$[f'(-5)] = \lim_{h \rightarrow 0} \frac{f(-5+h) - f(-5)}{h} \xrightarrow{f(-5) = \frac{1}{2}} \lim_{h \rightarrow 0} \frac{\frac{1-h}{2} + h^2 - h^3 - \frac{1}{2}}{h} = \\ = \lim_{h \rightarrow 0} \frac{\cancel{h} - h + h^2 - h^3 - \cancel{h}}{2h} = \lim_{h \rightarrow 0} \frac{h(-1+h-h^2)}{2h} = \boxed{-\frac{1}{2}}$$

$$\text{Άρα } [f(-5) + f'(-5)] = \frac{1}{2} - \frac{1}{2} = [0]$$

14.7 5)

$$f(6+h) = 1933 + h - 3h^2 + h^5 \xrightarrow{h=0} f(6+0) = 1933 + 0 - 3 \cdot 0^2 + 0^5 \Rightarrow [f(6) = 1933]$$

Ακόμη

$$\boxed{f'(6)} = \lim_{h \rightarrow 0} \frac{f(6+h) - f(6)}{h} \stackrel{f(6)=1933}{=} \lim_{h \rightarrow 0} \frac{1933 + h - 3h^2 + h^5 - 1933}{h} =$$
$$= \lim_{h \rightarrow 0} \frac{h(1 - 3h + h^4)}{h} = \boxed{1}$$

$$\text{Answer } \boxed{f(6)} = 1933 = 1933 \cdot 1 = \boxed{1933f'(6)}$$