

Επειδή η f είναι παραγωγίσιμη στο $x_0 = 2$, θα ισχύει $\lim_{x \rightarrow 2} \frac{f(x) - f(2)}{x - 2} = f'(2)$

Οπότε

$$\begin{aligned} \boxed{g'(0)} &= \lim_{x \rightarrow 0} \frac{g(x) - g(0)}{x} \stackrel{g(x)=3f(x)+\frac{2x}{f(x)} \Rightarrow g(0)=3f(0)}{=} \lim_{x \rightarrow 0} \frac{3f(x) + \frac{2x}{f(x)} - 3f(0)}{x} = \\ &= \lim_{x \rightarrow 0} \frac{3f(x) - 3f(0)}{x} + \lim_{x \rightarrow 0} \frac{\cancel{2x} \cdot \frac{1}{\cancel{f(x)}}}{\cancel{x}} = 3 \lim_{x \rightarrow 0} \frac{f(x) - f(0)}{x} + 2 \lim_{x \rightarrow 0} \frac{1}{f(x)} = \\ &\stackrel{\lim_{x \rightarrow 0} \frac{f(x) - f(0)}{x} = f'(0)}{=} \lim_{x \rightarrow 0} f(x) = f(0) \text{ (διότι } f \text{ παραγωγίσιμη, άρα συνεχής)} \stackrel{f'(0)=4}{=} 3 \cdot 4 + 2 \cdot \frac{1}{f(0)=2} = \boxed{13} \end{aligned}$$