

$$f(x) = \frac{1}{1-x} \Rightarrow f(f(x)) = \frac{1}{1-f(x)} \xrightarrow{f(x)=\frac{1}{1-x}} f(f(x)) = \frac{1}{1-\frac{1}{1-x}} \Rightarrow f(f(x)) = \frac{1}{\cancel{1-x}-\cancel{1}} \Rightarrow$$

$$\Rightarrow f(f(x)) = \frac{1-x}{-x} \Rightarrow f(f(x)) = \frac{x-1}{x}$$

Οπότε

$$f(f(x)) = \frac{x-1}{x} \Rightarrow f(f(f(x))) = \frac{f(x)-1}{f(x)} \xrightarrow{f(x)=\frac{1}{1-x}} f(f(f(x))) = \frac{\frac{1}{1-x}-1}{\frac{1}{1-x}} \Rightarrow$$

$$\Rightarrow f(f(f(x))) = \frac{\cancel{1}-\cancel{1}+x}{\frac{\cancel{1-x}}{1}} \Rightarrow f(f(f(x))) = x$$